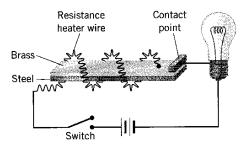
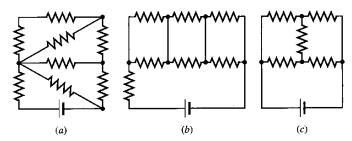
- 7. Often, the instructions for an electrical appliance do not state how many watts of power the appliance uses. Instead, a statement such as "10 A, 120 V" is given. Explain why this statement is equivalent to telling you the power consumption.
- drawing **8.** The shows a circuit that includes a bimetallic strip (made from brass and steel, see Section 12.4) with a resistance heater wire wrapped around it.



When the switch is initially closed, a current appears in the circuit, because charges flow through the heater wire (which becomes hot), the strip itself, the contact point, and the light bulb. The bulb glows in response. As long as the switch remains closed, does the bulb continue to glow, eventually turn off permanently, or flash on and off? Account for your answer.

- 9. The power rating of a 1000-W heater specifies the power consumed when the heater is connected to an ac voltage of 120 V. Explain why the power consumed by two of these heaters connected in series with a voltage of 120 V is not 2000 W.
- 10. A number of light bulbs are to be connected to a single electrical outlet. Will the bulbs provide more brightness if they are connected in series or in parallel? Why?

- 11. A car has two headlights. The filament of one burns out. However, the other headlight stays on. Draw a circuit diagram that shows how the lights are connected to the battery. Give your reasoning.
- 12. In one of the circuits in the drawing, none of the resistors is in series or in parallel. Which is it? Explain.



- 13. You have four identical resistors, each with a resistance of R. You are asked to connect these four together so that the equivalent resistance of the resulting combination is R. How many ways can you do it? There is more than one way. Justify your answers.
- 14. Compare the resistance of an ideal ammeter with the resistance of an ideal voltmeter and explain why the resistances are so different.
- 15. Describe what would happen to the current in a circuit if a voltmeter, inadvertently mistaken for an ammeter, were inserted into the circuit.
- 16. The time constant of a series RC circuit is  $\tau = RC$ . Verify that an ohm times a farad is equivalent to a second.

# PROBLEMS

Note: For problems that involve ac conditions, the current and voltage are rms values and the power is an average value, unless indicated otherwise.

ssm Solution is in the Student Solutions Manual. www Solution is available on the World Wide Web at http://www.wiley.com/college/cutnell 

#### Section 20.1 Electromotive Force and Current, Section 20.2 Ohm's Law

- 1. ssm A portable compact disc player is designed to play for 2.0 h on a fully charged battery pack. If the battery pack provides a total of 180 C of charge, how much current does the player use in operating?
- & 2. A defibrillator is used during a heart attack to restore the heart to its normal beating pattern (see Section 19.5). A defibrillator passes 18 A of current through the torso of a person in 2.0 ms. (a) How much charge moves during this time? (b) How many electrons pass through the wires connected to the patient?
  - 3. The filament of a light bulb has a resistance of 580  $\Omega$ . A voltage of 120 V is connected across the filament. How much current is in the filament?
  - outlet. What is the current in the toaster?

- 5. ssm The heating element of a clothes drier has a resistance of 11  $\Omega$  and is connected across a 240-V electrical outlet. What is the current in the heating element?
- 6. A battery charger is connected to a dead battery and delivers a current of 6.0 A for 5.0 hours, keeping the voltage across the battery terminals at 12 V in the process. How much energy is delivered to the battery?
- \*7. The resistance of a bagel toaster is 14  $\Omega$ . To prepare a bagel, the toaster is operated for one minute from a 120-V outlet. How much energy is delivered to the toaster?
- 6 \*8. A car battery has a rating of 220 ampere hours (A ⋅ h). This rating is one indication of the total charge that the battery can provide to a circuit before failing. (a) What is the total charge (in coulombs) that this battery can provide? (b) Determine the maximum current that the battery can provide for 38 minutes.
- 4. A toaster has a resistance of 14  $\Omega$  and is plugged into a 120-V  $\flat$ \*\*9. ssm A beam of protons is moving toward a target in a particle accelerator. This beam constitutes a current whose value is

 $0.50 \mu A$ . (a) How many protons strike the target in 15 seconds? (b) Each proton has a kinetic energy of  $4.9 \times 10^{-12}$  J. Suppose the target is a 15-gram block of aluminum, and all the kinetic energy of the protons goes into heating it up. What is the change in temperature of the block at the end of 15 s?

#### Section 20.3 Resistance and Resistivity

- 6 10. High-voltage power lines are a familiar sight throughout the country. The aluminum wire used for some of these lines has a cross-sectional area of  $4.9 \times 10^{-4}$  m<sup>2</sup>. What is the resistance of ten kilometers of this wire?
  - 11. ssm www Two wires have the same length and the same resistance. One is made from aluminum and the other from copper. Obtain the ratio of the cross-sectional area of the aluminum wire to that of the copper wire.
  - 12. A coil of wire has a resistance of 38.0  $\Omega$  at 25 °C and 43.7  $\Omega$  at 55 °C. What is the temperature coefficient of resistivity?
  - 13. A cylindrical copper cable carries a current of 1200 A. There is a potential difference of  $1.6 \times 10^{-2} \, \mathrm{V}$  between two points on the cable that are 0.24 m apart. What is the radius of the cable?
  - 14. A cylindrical wire of length 2.80 m and radius 1.03 mm carries a current of 1.35 A. The voltage across the ends of the wire is 0.0320 V. From what material in Table 20.1 is the wire made?
- $\checkmark$  15. A wire of unknown composition has a resistance of  $R_0$  = 35.0 Ω when immersed in water at 20.0 °C. When the wire is placed in boiling water, its resistance rises to 47.6  $\Omega$ . What is the temperature of a hot summer day when the wire has a resistance of 37.8  $\Omega$ ?
- \*16. A tungsten wire has a radius of 0.075 mm and is heated from 20.0 to 1320 °C. The temperature coefficient of resistivity is  $\alpha = \frac{1}{2}$  \*27. \*5m Tungsten has a temperature coefficient of resistivity of  $4.5 \times 10^{-3} \, (\text{C}^{\circ})^{-1}$ . When 120 V is applied across the ends of the hot wire, a current of 1.5 A is produced. How long is the wire? Neglect any effects due to thermal expansion.
- \*17. ssm www A wire has a resistance of 21.0  $\Omega$ . It is melted down, and from the same volume of metal a new wire is made that is three times longer than the original wire. What is the resistance of the new wire?
- \*18. A toaster uses a Nichrome heating wire. When the toaster is turned on at 20 °C, the initial current is 1.50 A. A few seconds later, the toaster warms up and the current has a value of 1.30 A. The average temperature coefficient of resistivity for Nichrome wire is  $4.5 \times 10^{-4} \, (\text{C}^{\circ})^{-1}$ . What is the temperature of the heating wire?
- \*19. ssm www Two wires have the same cross-sectional area and are joined end to end to form a single wire. One is tungsten, which has a temperature coefficient of resistivity of  $\alpha = 0.0045 \text{ (C}^{\circ})^{-1}$ . The other is carbon, for which  $\alpha =$ -0.0005 (C°)<sup>-1</sup>. The total resistance of the composite wire is the sum of the resistances of the pieces. The total resistance of the composite does not change with temperature. What is the ratio of the lengths of the tungsten and carbon sections? Ignore any changes in length due to thermal expansion.
- \*\* 20. An aluminum wire is hung between two towers and has a length of 175 m. A current of 125 A exists in the wire, and the

potential difference between the ends of the wire is 0.300 V. The density of aluminum is 2700 kg/m<sup>3</sup>. Find the mass of the wire.

#### **Section 20.4 Electric Power**

- 21. An automobile battery is being charged at a voltage of 12.0 V and a current of 19.0 A. How much power is being produced by the charger?
- 22. A cigarette lighter in a car is a resistor that, when activated, is connected across the 12-V battery. Suppose a lighter dissipates 33 W of power. Find (a) the resistance of the lighter and (b) the current that the battery delivers to the lighter.
- 23. ssm In doing a load of clothes, a clothes drier uses 16 A of current at 240 V for 45 min. A personal computer, in contrast, uses 2.7 A of current at 120 V. With the energy used by the clothes drier, how long (in hours) could you use this computer to "surf" the internet?
- 24. There are approximately 110 million TVs in the United States. Each uses, on average, 75 W of power and is turned on for 6.0 hours a day. If electrical energy costs \$0.10 per KWh, how much money is spent every day in keeping the TVs turned on?
- 25. An electric blanket is connected to a 120-V outlet and consumes 140 W of power. What is the current in the wire in the blanket?
- 26. A blow-drier and a vacuum cleaner each operate with an ac voltage of 120 V. The current rating of the blow-drier is 11 A, while that of the vacuum cleaner is 4.0 A. Determine the power consumed by (a) the blow-drier and (b) the vacuum cleaner. (c) Determine the ratio of the energy used by the blow-drier in 15 minutes to the energy used by the vacuum cleaner in one-half an hour.
- 0.0045 (C°)<sup>-1</sup>. A tungsten wire is connected to a source of constant voltage via a switch. At the instant the switch is closed, the temperature of the wire is 28 °C, and the initial power dissipated in the wire is  $P_0$ . At what wire temperature has the power dissipated in the wire decreased to  $\frac{1}{2}P_0$ ?
- \*28. A piece of Nichrome wire has a radius of  $6.5 \times 10^{-4}$  m. It is used in a laboratory to make a heater that dissipates 4.00 × 10<sup>2</sup> W of power when connected to a voltage source of 120 V. Ignoring the effect of temperature on resistance, estimate the necessary length of wire.
- **\*\*29.** An iron wire has a resistance of 12  $\Omega$  at 20.0 °C and a mass of  $1.3 \times 10^{-3}$  kg. A current of 0.10 A is sent through the wire for one minute and causes the wire to become hot. Assuming that all the electrical energy is dissipated in the wire and remains there, find the final temperature of the wire. (Hint: Use the average resistance of the wire during the heating process, and see Table 12.2 for the specific heat capacity of iron. Note  $\alpha = 0.0050 \, (\text{C}^{\circ})^{-1}$ .)

#### Section 20.5 Alternating Current

- 30. The average power dissipated in a stereo speaker is 55 W. Assuming that the speaker can be treated as a 4.0- $\Omega$  resistance, find the peak value of the ac voltage applied to the speaker.
- 31. The current in a circuit is ac and has a peak value of 2.50 A. Determine the rms current.

- 32. A light bulb is connected to a 120.0-V wall socket. The current in the bulb depends on the time t according to the relation I = (0.707 A)sin [(314 Hz)t], where the peak current is 0.707 A.
  (a) What is the frequency of the alternating current? (b) Determine the resistance of the bulb's filament. (c) What is the average power consumed by the light bulb?
- 33. ssm The heating element in an iron has a resistance of  $16 \Omega$  7\*45. Three resistors are connected in series across a battery. The and is connected to a 120-V wall socket. (a) What is the average power consumed by the iron, and (b) the peak power? Value of each resistance and its maximum power rating are as follows: 5.0  $\Omega$  and 20.0 W. 30.0  $\Omega$  and 10.0 W. and 15.0  $\Omega$  and
  - 34. Review Conceptual Example 7 as an aid in solving this problem. A portable electric heater uses 18 A of current. The manufacturer recommends that an extension cord attached to the heater dissipates no more than 2.0 W of power per meter of length. What is the smallest radius of copper wire that can be used in the extension cord? (Note: An extension cord contains two wires.)
  - 35. An electric furnace runs nine hours a day to heat a house during January (31 days). The heating element has a resistance of 5.3  $\Omega$  and carries a current of 25 A. The cost of electricity is \$0.10/kWh. Find the monthly cost of running the furnace.
- \*36. On its highest setting, a heating element on an electric stove (see Figure 20.9) is connected to an ac voltage of 240 V. This element has a resistance of 29  $\Omega$ . (a) Find the power dissipated in the element. (b) Assuming that three-fourths of the heat produced by the element is used to heat a pot of water (the rest being wasted), find the time required to bring 1.9 kg of water (half a gallon) at 15 °C to a boil.
- \*37. ssm The recovery time of a hot water heater is the time required to heat all the water in the unit to the desired temperature. Suppose that a 52-gal (1.00 gal =  $3.79 \times 10^{-3}$  m³) unit starts with cold water at 11 °C and delivers hot water at 53 °C. The unit is electric and utilizes a resistance heater (120 V ac, 3.0  $\Omega$ ) to heat the water. Assuming that no heat is lost to the environment, determine the recovery time (in hours) of the unit.
- \*\*38. To save on heating costs, the owner of a green house keeps 660 kg of water around in barrels. During a winter day, the water is heated by the sun to 10.0 °C. During the night the water freezes into ice at 0.0 °C in nine hours. What is the minimum ampere rating of an electric heating system (240 V) that would provide the same heating effect as the water does?

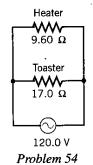
#### **Section 20.6 Series Wiring**

- 7 39. ssm Three resistors, 25, 45, and 75  $\Omega$ , are connected in series, and a 0.51-A current passes through them. What is (a) the equivalent resistance and (b) the potential difference across the three resistors?
  - **40.** The current in a 47- $\Omega$  resistor is 0.12 A. This resistor is in series with a 28- $\Omega$  resistor, and the series combination is connected across a battery. What is the battery voltage?
  - 41. A 36.0- $\Omega$  resistor and an 18.0- $\Omega$  resistor are connected in series across a 15.0-V battery. What is the voltage across (a) the \*55. ssm The total current delivered to a 36.0- $\Omega$  resistor and (b) the 18.0- $\Omega$  resistor?
  - **42.** A 60.0-W lamp is placed in series with a resistor and a 120.0-V source. If the voltage across the lamp is 25 V, what is the resistance R of the resistor?

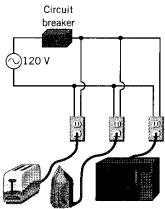
- **43. ssm** The current in a series circuit is 15.0 A. When an additional  $8.00-\Omega$  resistor is inserted in series, the current drops to 12.0 A. What is the resistance in the original circuit?
- 44. Three resistors, 9.0, 5.0, and 1.0  $\Omega$ , are connected in series across a 24-V battery. Find (a) the current in, (b) the voltage across, and (c) the power dissipated in each resistor.
- \*45. Three resistors are connected in series across a battery. The value of each resistance and its maximum power rating are as follows: 5.0  $\Omega$  and 20.0 W, 30.0  $\Omega$  and 10.0 W, and 15.0  $\Omega$  and 10.0 W. (a) What is the greatest voltage that the battery can have without one of the resistors burning up? (b) How much power does the battery deliver to the circuit in (a)?
- \*46. One heater uses 340 W of power when connected by itself to a battery. Another heater uses 240 W of power when connected by itself to the same battery. How much total power do the heaters use when they are both connected in series across the battery?
- \*\*47. Two resistances,  $R_1$  and  $R_2$ , are connected in series across a 12-V battery. The current increases by 0.20 A when  $R_2$  is removed, leaving  $R_1$  connected across the battery. However, the current increases by just 0.10 A when  $R_1$  is removed, leaving  $R_2$  connected across the battery. Find (a)  $R_1$  and (b)  $R_2$ .

#### Section 20.7 Parallel Wiring

- **48.** What resistance must be placed in parallel with a 155- $\Omega$  resistor to make the equivalent resistance 115  $\Omega$ ?
- 49. ssm A  $16-\Omega$  loudspeaker and an  $8.0-\Omega$  loudspeaker are connected in parallel across the terminals of an amplifier. Assuming the speakers behave as resistors, determine the equivalent resistance of the two speakers.
- **50.** For the 3-way bulb (50 W, 100 W, 150 W) discussed in Conceptual Example 10, find the resistance of each of the two filaments. Assume that the wattage ratings are not limited by significant figures and ignore any heating effects on the resistances.
- **51. ssm** Two resistors, 42.0 and 64.0  $\Omega$ , are connected in parallel. The current through the 64.0- $\Omega$  resistor is 3.00 A. (a) Determine the current in the other resistor. (b) What is the total power consumed by the two resistors?
- **52.** A wire whose resistance is R is cut into three equally long pieces, which are then connected in parallel. In terms of R, what is the resistance of the parallel combination?
- 53. A coffee cup heater and a lamp are connected in parallel to the same 120-V outlet. Together, they use a total of 84 W of power. The resistance of the heater is  $6.0 \times 10^2 \ \Omega$ . Find the resistance of the lamp.
- **54.** The drawing shows an electric heater  $(R = 9.60 \Omega)$  and a toaster  $(R = 17.0 \Omega)$ . (a) What is the voltage across the heater? (b) Determine the current in the toaster. (c) What is the total power supplied to the heater and the toaster?
- number of devices connected in parallel is the sum of the individual currents in each device. Circuit breakers are resettable automatic switches that protect against a dangerously



large total current by "opening" to stop the current at a specified safe value. A 1650-W toaster, a 1090-W iron, and a 1250-W microwave oven are turned on in a kitchen. As the drawing shows, they are all connected through a 20-A circuit breaker to an ac voltage of 120 V. (a) Find the equivalent resistance of the three devices. (b) Obtain the total current delivered by the source

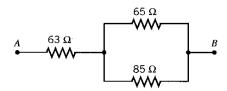


and determine whether the breaker will "open" to prevent an accident.

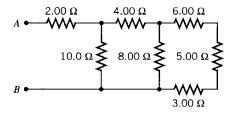
- \*56. A resistor (resistance = R) is connected first in parallel and then in series with a 2.00- $\Omega$  resistor. A battery delivers five times as much current to the parallel combination than it does to the series combination. Determine the two possible values for R.
- \*\*57. The rear window defogger of a car consists of thirteen thin wires (resistivity =  $88.0 \times 10^{-8} \ \Omega \cdot m$ ) embedded in the glass. The wires are connected in parallel to the 12.0-V battery, and each has a length of 1.30 m. The defogger can melt  $2.10 \times 10^{-2} \ kg$  of ice at 0 °C into water at 0 °C in two minutes. Assume that all the power dissipated in the wires is used immediately to melt the ice. Find the cross-sectional area of each wire.

# Section 20.8 Circuits Wired Partially in Series and Partially in Parallel

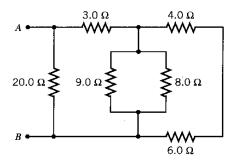
- **58.** A 14- $\Omega$  coffee maker and a 16- $\Omega$  frying pan are connected in series across a 120-V source of voltage. A 23- $\Omega$  bread maker is also connected across the 120-V source and is in parallel with the series combination. Find the total current supplied by the source of voltage.
- **59. ssm** For the combination of resistors shown in the drawing, determine the equivalent resistance between points A and B.



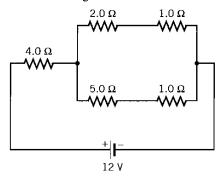
**60.** Find the equivalent resistance between points A and B in the drawing.



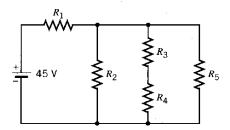
**61. ssm** Determine the equivalent resistance between the points A and B for the group of resistors in the drawing.



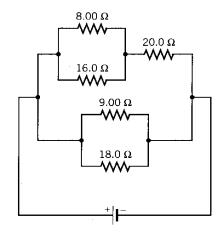
- **62.** A 60.0- $\Omega$  resistor is connected in parallel with a 120.0- $\Omega$  resistor. This parallel group is connected in series with a 20.0- $\Omega$  resistor. The total combination is connected across a 15.0-V battery. Find (a) the current and (b) the power dissipated in the 120.0- $\Omega$  resistor.
- 7\*63. Determine the power dissipated in the 5.0- $\Omega$  resistor in the circuit shown in the drawing.



\*64. The circuit in the drawing contains five identical resistors. The 45-V battery delivers 58 W of power to the circuit. What is the resistance R of each resistor?



\*65. ssm www The current in the 8.00- $\Omega$  resistor in the drawing is 0.500 A. Find the current in (a) the 20.0- $\Omega$  resistor and in (b) the 9.00- $\Omega$  resistor.



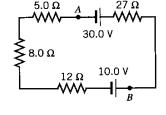
\*\*66. Three identical resistors are connected in parallel. The equivalent resistance increases by 700  $\Omega$  when one resistor is removed and connected in series with the remaining two, which are still in parallel. Find the resistance of each resistor.

#### **Section 20.9 Internal Resistance**

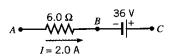
- 767. A 1.40- $\Omega$  resistor is connected across a 9.00-V battery. The voltage between the terminals of the battery is observed to be only 8.30 V. Find the internal resistance of the battery.
  - **68.** A new "D" battery has an emf of 1.5 V. When a wire of negligible resistance is connected between the terminals of the battery, a current of 28 A is produced. Find the internal resistance of the battery.
- **69. ssm** A battery has an internal resistance of 0.50  $\Omega$ . A number of identical light bulbs, each with a resistance of 15  $\Omega$ , are connected in parallel across the battery terminals. The terminal voltage of the battery is observed to be one-half the emf of the battery. How many bulbs are connected?
  - 70. A battery delivering a current of 55.0 A to a circuit has a terminal voltage of 23.4 V. The electric power being dissipated by the internal resistance of the battery is 34.0 W. Find the emf of the battery.
  - 71. A battery has an emf of 12.0 V and an internal resistance of 0.15  $\Omega$ . What is the terminal voltage when the battery is connected to a 1.50- $\Omega$  resistor?
  - \*72. A 75.0- $\Omega$  and a 45.0- $\Omega$  resistor are connected in parallel. When this combination is connected across a battery, the current delivered by the battery is 0.294 A. When the 45.0- $\Omega$  resistor is disconnected, the current from the battery drops to 0.116 A. Determine (a) the emf and (b) the internal resistance of the battery.

#### Section 20.10 Kirchhoff's Rules

73. ssm Consider the circuit in the drawing. Determine (a) the magnitude of the current in the circuit and (b) the magnitude of the voltage between the points labeled A and B. (c) State which point, A or B, is at the higher potential.

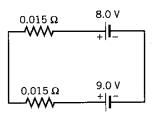


74. A current of 2.0 A exists in the partial circuit shown in the drawing. What is the magnitude of the potential difference between the points (a) A and B, and (b) A and C?

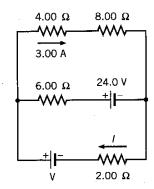


75. Two batteries, each with an internal resistance of 0.015  $\Omega$ , are connected as in the drawing. In effect, the 9.0-V battery is being used to charge the 8.0-V battery. What is the current in the cir-

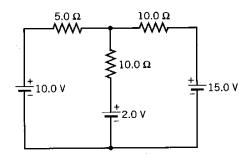
cuit?



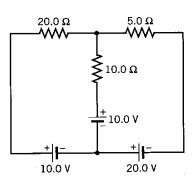
76. For the circuit shown in the drawing, find the current I through the 2.00- $\Omega$  resistor and the voltage V of the battery to the left of this resistor.



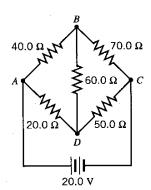
\*77. ssm Determine the voltage across the  $5.0-\Omega$  resistor in the drawing. Which end of the resistor is at the higher potential?



\*78. For the circuit in the drawing, find the current in the 10.0- $\Omega$  resistor. Specify the direction of the current.



\*\*79. The circuit in the drawing is known as a Wheatstone bridge circuit. Find the voltage between points B and D, and state which point is at the higher potential.

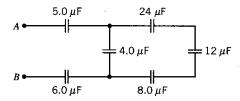


#### Section 20.11 The Measurement of Current and Voltage

- 80. A galvanometer has a full-scale current of 0.100 mA and a coil resistance of 50.0  $\Omega$ . This instrument is used with a shunt resistor to form an ammeter that will register full scale for a current of 60.0 mA. Determine the resistance of the shunt resistor.
- 81. ssm A voltmeter utilizes a galvanometer that has a  $180-\Omega$  coil resistance and a full-scale current of 8.30 mA. The voltmeter measures voltages up to 30.0 V. Determine the resistance that is connected in series with the galvanometer.
- 82. The coil of a galvanometer has a resistance of  $20.0 \Omega$ , and its meter deflects full scale when a current of 6.20 mA passes through it. To make the galvanometer into an ammeter, a  $24.8\text{-m}\Omega$  shunt resistor is added to it. What is the maximum current that this ammeter can read?
- 83. The equivalent resistance of a voltmeter is 140 000  $\Omega$ . The voltmeter uses a galvanometer that has a full-scale current of 180  $\mu$ A. What is the maximum voltage that can be measured by the voltmeter?
- \*84. Two scales on a voltmeter measure voltages up to 20.0 and 30.0 V, respectively. The resistance connected in series with the galvanometer is 1680  $\Omega$  for the 20.0-V scale and 2930  $\Omega$  for the 30.0-V scale. Determine the coil resistance and the full-scale current of the galvanometer that is used in the voltmeter.
- \*\*85. ssm In measuring a voltage, a voltmeter uses some current from the circuit. Consequently, the voltage measured is only an approximation to the voltage present when the voltmeter is not connected. Consider a circuit consisting of two 1550-Ω resistors connected in series across a 60.0-V battery. (a) Find the voltage across one of the resistors. (b) A voltmeter has a full-scale voltage of 60.0 V and uses a galvanometer with a full-scale deflection of 5.00 mA. Determine the voltage that this voltmeter registers when it is connected across the resistor used in part (a).

#### Section 20.12 Capacitors in Series and Parallel

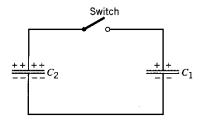
- **86.** A 4.0- $\mu$ F and an 8.0- $\mu$ F capacitor are connected in parallel across a 25-V battery. Find (a) the equivalent capacitance and (b) the total charge stored on the two capacitors.
- 7 87. Determine the equivalent capacitance between A and B for the group of capacitors in the drawing.



88

Three capacitors (4.0, 6.0, and 12.0  $\mu$ F) are connected in series across a 50.0-V battery. Find the voltage across the 4.0- $\mu$ F capacitor.

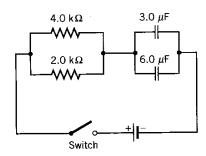
- 7 89. ssm A 3.0-μF capacitor and a 4.0-μF capacitor are connected in series across a 40.0-V battery. A 10.0-μF capacitor is also connected directly across the battery terminals. Find the total charge that the battery delivers to the capacitors.
  - **90.** Three capacitors have identical geometries. One is filled with a material whose dielectric constant is 2.50. Another is filled with a material whose dielectric constant is 4.00. The third capacitor is filled with a material whose dielectric constant  $\kappa$  is such that this single capacitor has the same capacitance as the series combination of the other two. Determine  $\kappa$ .
  - 91. Suppose two capacitors  $(C_1 \text{ and } C_2)$  are connected in series. Show that the sum of the energies stored in these capacitors is equal to the energy stored in the equivalent capacitor. [Hint: The energy stored in a capacitor can be expressed as  $q^2/(2C)$ .]
- \*92. A 3.00- $\mu$ F and a 5.00- $\mu$ F capacitor are connected in series across a 30.0-V battery. A 7.00- $\mu$ F capacitor is then connected in parallel across the 3.00- $\mu$ F capacitor. Determine the voltage across the 7.00- $\mu$ F capacitor.
- \*93. ssm A 7.0- $\mu$ F and a 3.0- $\mu$ F capacitor are connected in series across a 24-V battery. What voltage is required to charge a parallel combination of the two capacitors to the same total energy?
- \*\*94. The drawing shows two fully charged capacitors ( $C_1 = 2.00~\mu\text{F}$ ,  $q_1 = 6.00~\mu\text{C}$ ;  $C_2 = 8.00~\mu\text{F}$ ,  $q_2 = 12.0~\mu\text{C}$ ). The switch is closed, and charge flows until equilibrium is reestablished (i.e., until both capacitors have the same voltage across their plates). Find the resulting voltage across either capacitor.



#### Section 20.13 RC Circuits

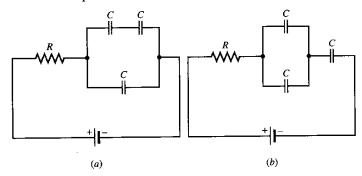
- 95. ssm  $\leq$  In a heart pacemaker, a pulse is delivered to the heart 81 times per minute. The capacitor that controls this pulsing rate discharges through a resistance of  $1.8 \times 10^6 \Omega$ . One pulse is delivered every time the fully charged capacitor loses 63.2% of its original charge. What is the capacitance of the capacitor?
- 96. An electronic flash attachment for a camera produces a flash by using the energy stored in a  $750-\mu F$  capacitor. Between flashes, the capacitor recharges through a resistor whose resistance is chosen so the capacitor recharges with a time constant of 3.0 s. Determine the value of the resistance.
- 97. The circuit in the drawing contains two resistors and two capacitors that are connected to a battery via a switch. When the

switch is closed, the capacitors begin to charge up. What is the time constant for the charging process?



\*98. Three identical capacitors are connected with a resistor in two different ways. When they are connected as in part a of the drawing, the time constant to charge up this circuit is 0.34 s.

What is the time constant when they are connected with the same resistor as in part b?



\*\*99. How many time constants must elapse before a capacitor in a series RC circuit is charged to within 0.10% of its equilibrium charge?

# ADDITIONAL PROBLEMS

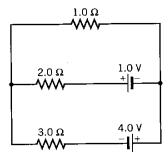
100. The heating element in an iron has a resistance of 24  $\Omega$ . The iron is plugged into a 120-V outlet. What is the power dissipated by the iron?

**101.** ssm Three capacitors (3.0, 7.0, and 9.0  $\mu$ F) are connected in series. What is their equivalent capacitance?

102. A lightning bolt delivers a charge of 35 C to the ground in a time of  $1.0 \times 10^{-3}$  s. What is the current?

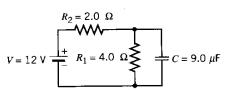
103. ssm In the arctic, electric socks are useful. A pair of socks uses a 9.0-V battery pack for each sock. A current of 0.11 A is drawn from each battery pack by wire woven into the socks. Find the resistance of the wire in one sock.

104. Find the magnitude and direction of the current in the  $2.0\text{-}\Omega$  resistor in the drawing.



105. In Section 12.3 it was mentioned that temperatures are often measured with electrical resistance thermometers made of platinum wire. Suppose that the resistance of a platinum resistance thermometer is 125  $\Omega$  when its temperature is 20.0 °C. The wire is then immersed in boiling chlorine, and the resistance drops to 99.6  $\Omega$ . The temperature coefficient of resistivity of platinum is  $\alpha = 3.72 \times 10^{-3} \, (\text{C}^{\circ})^{-1}$ . What is the temperature of the boiling chlorine?

106. The circuit in the drawing shows two resistors, a capacitor, and a battery. When the capacitor is fully charged, what is the magnitude q of the charge on one of its plates?



107. A galvanometer with a coil resistance of 12.0  $\Omega$  and a full-scale current of 0.150 mA is used with a shunt resistor to make an ammeter. The ammeter registers a maximum current of 4.00 mA. Find the equivalent resistance of the ammeter.

\*108. Two cylindrical rods, one copper and the other iron, are identical in lengths and cross-sectional areas. They are joined, end-to-end, to form one long rod. A 12-V battery is connected across the free ends of the copper-iron rod. What is the voltage between the ends of the copper rod?

\*109. ssm Eight different values of resistance can be obtained by connecting together three resistors (1.00, 2.00, and 3.00  $\Omega$ ) in all possible ways. What are they?

\*110. A cylindrical aluminum pipe of length 1.50 m has an inner radius of  $2.00 \times 10^{-3}$  m and an outer radius of  $3.00 \times 10^{-3}$  m. The interior of the pipe is completely filled with copper. What is the resistance of this unit? (Hint: Imagine that the pipe is connected between the terminals of a battery and decide whether the aluminum and copper parts of the pipe are in series or in parallel.)

\*111. ssm An extension cord is used with an electric weed trimmer that has a resistance of 15.0  $\Omega$ . The extension cord is made of copper wire that has a cross-sectional area of  $1.3 \times 10^{-6}$  m<sup>2</sup>.

The combined length of the two wires in the extension cord is 92 m. (a) Determine the resistance of the extension cord. (b) The extension cord is plugged into a 120-V socket. What voltage is applied to the trimmer itself?

- \*112. A resistor has a resistance R, and a battery has an internal resistance r. When the resistor is connected across the battery, ten percent less power is dissipated in R than there would be if the battery had no internal resistance. Find the ratio r/R.
- \*113. An iron wire has a resistance of 5.90  $\Omega$  at 20.0 °C, and a gold wire has a resistance of 6.70  $\Omega$  at the same temperature. The temperature coefficient of resistivity for iron is 0.0050 ( $C^{\circ}$ )<sup>-1</sup>, while for gold it is 0.0034 ( $C^{\circ}$ )<sup>-1</sup>. At what temperature do the wires have the same resistance?
- \*114. A 47- $\Omega$  resistor can dissipate up to 0.25 W of power without burning up. What is the smallest number of such resistors that

- can be connected in series across a 9.0-V battery without any one of them burning up?
- \*\*\* 115. **ssm** A sheet of gold foil (negligible thickness) is placed between the plates of a capacitor and has the same area as each of the plates. The foil is parallel to the plates, at a position one-third of the way from one to the other. Before the foil is inserted, the capacitance is  $C_0$ . What is the capacitance after the foil is in place? Express your answer in terms of  $C_0$ .
- \*\*116.  $\leq$  A digital thermometer uses a thermistor as the temperature-sensing element. A thermistor is a kind of semiconductor and has a large negative temperature coefficient of resistivity  $\alpha$ . Suppose  $\alpha = -0.060 \, (\text{C}^{\circ})^{-1}$  for the thermistor in a digital thermometer used to measure the temperature of a patient. The resistance of the thermistor decreases to 85% of its value at the normal body temperature of 37.0 °C. What is the patient's temperature?

## CONCEPTS

Ω

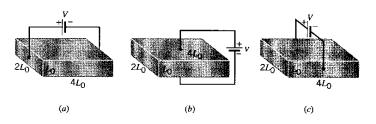
CALCULATIONS

## GROUP LEARNING PROBLEMS

Note: Each of these problems consists of Concept Questions followed by a related quantitative Problem. They are designed for use by students working alone or in small learning groups. The Concept Questions involve little or no mathematics and are intended to stimulate group discussions. They focus on the concepts with which the problems deal. Recognizing the concepts is the essential initial step in any problem-solving technique.

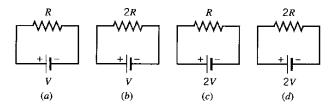
117. Concept Questions The resistance and the magnitude of the current depend on the path that the current takes. The drawing shows three situations in which the current takes different paths through a piece of material. Rank them according to (a) resistance and (b) current, largest first. Give your reasoning.

**Problem** Each of the rectangular pieces is made from a material whose resistivity is  $\rho = 1.50 \times 10^{-2} \, \Omega \cdot m$ , and the unit of length in the drawing is  $L_0 = 5.00$  cm. If the material is connected to a 3.00-V battery, find (a) the resistance and (b) the current in each case. Verify that your answers are consistent with your answers to the Concept Questions.



118. Concept Questions Each of the four circuits in the drawing consists of a single resistor whose resistance is either R or 2R, and a single battery whose voltage is either V or 2V. Rank the circuits according to (a) the power and (b) the current delivered to the resistor, largest to smallest. Explain your answers.

**Problem** The unit of voltage in each circuit is V = 12.0 V and the unit of resistance is  $R = 6.00 \Omega$ . Determine (a) the power dissipated in each resistor and (b) the current delivered to each resistor. Check to see that your answers are consistent with your answers to the Concept Questions.



119. Concept Questions The drawing shows three different resistors in two different circuits. The resistances are such that  $R_1 > R_2 > R_3$ . (a) For the circuit on the left, rank the current through each resistor and the voltage across each one, largest first. (b) Repeat part (a) for the circuit on the right. Justify your answers.

**Problem** The battery has a voltage of V=24.0 V, and the resistors have values of  $R_1=50.0$   $\Omega$ ,  $R_2=25.0$   $\Omega$ , and  $R_3=10.0$   $\Omega$ . (a) For the circuit on the left, determine the current through and the voltage across each resistor. (b) Repeat part (a) for the circuit on the right. Be sure your answers are consistent with your answers to the Concept Questions.

